

SMARTWING/EMORPH MEETING, IMFT- TOULOUSE, 30 MARCH 2012

Fondation de Coopération Scientifique Sciences et Technologies pour l'Aéronautique et l'Espace



RTRA-SMARTWING and EMORPH meeting

RTRA – « Réseau Thématique de Recherche Avancée »

The platform ('chantier') SMARTWING «New concepts for improving the aerodynamic performances of airvehicles»

Introductory presentation by

Marianna BRAZA

IMFT-CNRS

Research Team: "Interaction Fluide –Structure Sous Turbulence" - IFS2T Research Group "EMT2" Ecoulements Monophasiques, Transitionnels et Turbulents"

PARTNERS SMARTWING

•ISAE

•LAPLACE

•ONERA

•IMT









• IMFT - Coordonnateur



PROJECT : 01/02/2012- 28/02/2015

PARTNERS RTRA – EMMAV – Electroactive Morphing for Micro-Airvehicles : 1/01/2010-1/10/2012

•ISAE







•IMFT - Coordonnateur



PROJECT : 01/2010- 30/10/2012



Fondation de Coopération Scientifique Sciences et Technologies pour l'Aéronautique et l'Espace

RTRA – « Réseau Thématique de Recherche Avancée »

- Research program EMMAV Electroactive Morphing for Micro-Airvehicles
 2009-2012 IMFT, ISAE, LAPLACE
- 1) Research <u>PLATFORM</u> **SMARTWING** including :

2012-2015

Research program **DYNAMORPH**

4 workshops

SMARTWING MORPHING CENTRE

1 international conference June 2013

IMFT, IMT, ISAE, LAPLACE, ONERA

« The SMARTWING platform focuses on creation of a multi-disciplinary structure, associating the competences of the Toulouse laboratories in the domains of **aerodynamics, aeroelasticity, novel smart materials and of flight control commands**, to improve the aerodynamic efficiency of new generation of air-vehicles, by means of **Electroactive Morphing**"

OBJECTIVES and ORIGINAL ASPECTS IN THE STATE OF THE ART ELECTROACTIVE MORPHING

Shape optimisation for increasing performance and controlling instabilities and aerodynamic noise

- Optimisation of aerodynamic efficiency
- Real time: <u>Controller Design</u>
- Low energetic cost : recuperation and redistribution of environning vibratory energy by smart E-materials
- Replacement of hydraulic systems by electrical ones
- Loads control manoeuvrability trailing-edge ailerons
- Attenuation of instabilities due to separation and to aeroelastic flutter and of aerodynamic noise due to trailing edge K-H vortices
- APPLICATION : drones, ailerons, flexible wings, UAV, rotor blades flying wing, active transonic bumps: laminar wing

Instabilities occurring in aeronautics





PREMIERE CARACTERISATION DE CONCEPTS D'ACTUATION INNOVANTS – MORPHING ELECTROACTIF







- •SMA Shape Memory Alloys
- •Distributed small piezo-actuators, No-MEMS
- •Electroactive Polymers
 - Low actuation cost thanks to:
 - Capacity of vibratory energy recuperation and restitution
 - Modification of the behavior laws of the Ematerial – solid structure

ELECTROACTIVE MORPHING

New aircraft generation with deformable wings and ailerons attending optimal shape in real time



☐ Ailerons, volets, gouvernes, rotors





Morphing Electroactif

- SHAPE CONTROLLER DESIGN
- FLIGHT CONTROL COMMANDS AND EVALUATION

α

- EXPERIMENTAL DEMONSTRATOR





The optimal form is a function of a and depends on M, Re flow regimes

Deformation is reached by continuously distributed E-materials according to optimum design shape 20^{ème} Congrès Français de Mécanique

Besançon, 29 août au 2 septembre 2011



ACTIVATION D'UNE VOILURE DEFORMABLE PAR DES CABLES D'AMF REPARTIS EN SURFACE



Publication Congrès Français de Mécanique, Besançon, sept. 2011

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PIEZOACTUATEURS PZT – MORPHING DU BORD DE FUITE DE VOLET/ AILERON



J. Scheller, J.F. Rouchon, M. Chinaud, D. Haribey 2012





Nanorotors coaxiaux: caractérisation et optimisation





- Montage expérimental sur nano-balance de précision
- Calcul Navier-Stokes par méthode MRF



FROM EMMAV TO SMARTWING/DYNAMORPH

II.Vers un démonstrateur de drone électroactivé

Concept 1 morphing gouverne EMMAV 2009-2012



Concept 2 commande têtes de rotors par muscles artificiels: **DYNAMORPH** 2011-2014













General concept SMARTWING/DYNAMORPH - Hybridation concept : Distributed small piezoactuators and Shape Memory Alloys - Low actuation cost thanks to:

capacity of vibratory energy recuperation and restitution



Onera / Systems Control & Flight Dynamics Dpt.

- Robotics, Artificial Intelligence & Systems
- Controller Design & Flight Control

bedded Systems Design & Controller Integration











- MAVION Mini Fixed Wing UAV (Cooperation with ISAE)
- Autonomous Systems Robotics Demonstrators







SATELLITE' RESEARCH PROGRAMS TO RTRA-EMMAV - DYNAMORPH



MIT, BROWN, CORNELL, TEXAS-AUSTIN Universities



□ ASPECTS NOVATEURS

S'appuyant sur la compréhension des enjeux acquise au cours du EMMAV: nécessité de diversifier les types d'actuations:

•mini-piezoactuateurs PZT : haute fréquence de morphing –régime dynamique

•polymères électroactivés IPMC : perspectives technologiques inédites

vers la <u>biomimétique</u>: augmentation des performances réduction du bruit aérodynamique

•couplage fort fluide - structure :

•actuations rapides de petite amplitude à des actuations lentes de forte amplitude : verrou physique à l'accession à des *gains de performances*

PROJET DYNAMORPH

•OPTIMISATION DE FORME DES AERONEFS (PALES, AILERONS)

ET DE LA MANOEUVRABILITE DES DRONES

A L'AIDE DE NOUVEAUX CONCEPTS DE MORPHING ET DE

LEUR HYBRIDATION

•matériaux de type composites ioniques :

micro-hélicoptères à rotors souples



□ ASPECTS NOVATEURS -suite

•couplage fort fluide - structure :

•actuations rapides de petite amplitude à des actuations lentes de forte amplitude : verrou physique à l'accession à des gains de performances
•Système d'ailerons de bord de fuite complexes: biomimétique
Augmentation de la portance en régime de faible vitesse



IMFT CONTRIBUTION

MODELING CFDSM : Computational Fluid Dynamics- Structural Mechanics

Unsteady aerodynamics and aeroelasticity: Challengies:

High-Reynolds number flows with thin shear-layer interfaces

- Wall flows:Turbulence onset from near-wall
- Near-wake modeling : Decisive for prediction ability of aerodynamic forces

•Nouveaux concepts de modélisation de la turbulence URANS - LES: cascade énergétique inverse – upscale turbulence modelling

•Prédiction améliorée d'un ordre de grandeur des coefficients aérodynamiques

Couplage fort entre la structure et le fluide: résolution simultanée des équations CFD-SM :
Modélisation d'ordre réduit pour des prédictions réalistes de modification de forme pour le design



Turbulence modelling

Organized Eddy Simulation:

Energy spectrum splitting for

Distinction between the structures to be resolved from those to be modeled

based on their organised coherent character



Hoarau, Braza, IUTAM Symp. Toulouse 2002 Braza, 2002, 2006, Notes on Num. Fluid Mech. vol. 81, vol. 94 Braza, Perrin, Hoarau, J. Fluids Struct. 2006 Bourguet, Braza, J. Fluids & Struct. 2008 Braza, Hunt, European Turb. Conf., 2011 OES



Phase-averaged decomposition – Navier-Stokes equations

$$U_{i}\left(x_{k},t\right) = \left\langle U_{i}\left(x_{k},t\right)\right\rangle + u_{i}\left(x_{k},t\right)$$

$$\langle u_i(x_k,t)\rangle = 0$$
 $\langle \langle U_i(x_k,t)\rangle \rangle = \langle U_i(x_k,t)\rangle$



Navier-Stokes equations in phase-averaged decomposition Modification of modelling $\langle u_i u_j \rangle$ to take into account non-equilibrium

Modelling of 3D stress-strain misalignment

Exp.Eigenvectors of turbulence stress anisotropy (-a) and of strain rate (S) tensors, 3CTRPIV



Anisotropic eddy-viscosity : tensorial definition

$$a \approx -\frac{C_{V\,i}}{\lambda_i^S} S_i = -SV \text{diag} \left(\frac{C_{V1}}{\lambda_1^S} \ \frac{C_{V2}}{\lambda_2^S} \ \frac{C_{V3}}{\lambda_3^S} \right) V^t \quad \text{where} \quad V = \left(v_1^S \ v_2^S \ v_3^S \right)$$

Tensorial eddy-viscosity (Bourguet, Braza et al., AIAA J., 2007, J. Fluids & Struct. 24 (8), (2008)

$$(\nu_{tt})_{ij} = (\nu_{td})_k (v_k^S)_i (v_k^S)_j \text{ with } (\nu_{td})_i = \frac{C_{Vi}}{2\lambda_i^S} k , \ C_{\mu_i} = \frac{C_{Vi}}{2} \frac{\varepsilon}{k\lambda_i^S}$$

 $\eta_i = \frac{k|\lambda_i^s|}{\varepsilon}$, vectorial version of $\eta = \frac{k||S||}{\varepsilon}$ mean flow/turbulent time scale rate

Turbulent stress constitutive law : generalisation of the Linear EVM

$$-\overline{u_i u_j} + \frac{2}{3} k \delta_{ij} = 2 \frac{S_{ik} (\nu_{tt})_{kj}}{2}$$

Generalisation of averaged Navier-Stokes momentum equations

$$\frac{DU_i}{Dt} = \frac{\partial}{\partial x_j} \left(2\nu S_{ij} + 2(\nu_{tt})_{kj} S_{ik} - \frac{2}{3}k\delta_{ij} \right) - \frac{1}{\rho} \frac{\partial P}{\partial x_i}$$



Anisotropic closure scheme : directional DRSM

•Transport equations for Cvi projection coefficients, for q = 1,2,3

$$\frac{DC_{Vq}}{Dt} = -\left(V_q\right)_{ij} \frac{Da_{ij}}{Dt} - a_{ij} \frac{D\left(V_q\right)_{ij}}{Dt} , \ \left(V_q\right)_{ij} = \left(v_q^S\right)_i \left(v_q^S\right)_j$$

•Projection of Speziale, Sarkar and Gatski second order closure scheme J. Fluid Mech., 227, 1991

$$\begin{aligned} \frac{DC_{Vq}}{Dt} &= \left(\frac{4}{3} + c_3^* II_a^{\frac{1}{2}} - c_3\right) (V_q)_{ij} S_{ij} + (2 - 2c_4) (V_q)_{ij} a_{ik} S_{jk} - \frac{c_2 \varepsilon}{k} (V_q)_{ij} a_{ik} a_{kj} \\ &+ (2 - 2c_5) (V_q)_{ij} a_{ik} \Omega_{jk} + (1 - c_1) \frac{\varepsilon}{k} C_{Vq} + (1 + c_1^*) C_{Vq} a_{ij} S_{ij} + \frac{c_2 II_a \varepsilon}{3k} \\ &+ \frac{2 (c_4 - 1)}{3} a_{ij} S_{ij} - a_{ij} \frac{D (V_q)_{ij}}{Dt} + D^{C_{Vq}} \end{aligned}$$

where c_i and c_i^* are SSG model constants

$$\hat{a}_{ij}\frac{D\left(V_q\right)_{ij}}{Dt} = -C_{V_r}V_r\frac{D\left(V_q\right)_{ij}}{Dt} = 0 \text{ and } D^{C_{V_q}} = \frac{\partial}{\partial x_i}\left(\left(\nu + \frac{\left(\nu_{tt}\right)_{ij}}{\sigma_{C_{V_q}}}\right)\frac{\partial C_{V_q}}{\partial x_j}\right)$$

A tensorial eddy-diffusion coefficient $C_{\mu,i}$ can be derived. For faster computations, can be assumed scalar with equivalent optimum values of order 0.02

Tensorial eddy-viscosity modeling: Ability of capturing negative production of turbulence kinetic energy regions - relaminarisation



 $\mathcal{P}_{ij} = \langle u_i u_j \rangle \partial \langle U_i \rangle / \partial x_j$



Modeled

Detached Eddy Simulation

Turbulent length scale: $l_{DES} = \min(l_{RANS}, C_{DES} \times \Delta)$ $\Delta = \max(\Delta x, \Delta y, \Delta z)$



> For Spalart-Allmaras* model: $l_{DES} = \min(d_w, C_{DES} \times \Delta)$

Augmentation of the dissipation term in the eddy-viscosity transport equation:

$$\frac{D\,\widetilde{\nu}}{Dt} = c_{b1}(1 - f_{t2})\widetilde{S}\,\widetilde{\nu} + \frac{1}{\sigma} \Big[\nabla \cdot ((\nu + \widetilde{\nu})\nabla\,\widetilde{\nu}) + c_{b2}(\nabla\,\widetilde{\nu})^2\Big] - \left(C_{w1}f_w - \frac{C_{b1}}{\kappa^2}f_{t2}\right) \left(\frac{\widetilde{\nu}}{l_{DES}}\right)^2$$

> For k-
$$\omega$$
 ** model: $l_{DES} = \min(k^{1/2} / \beta \omega, C_{DES} \times \Delta)$

 \rightarrow Augmentation of the dissipation term in the k transport equation:

$$\frac{\overline{D\rho k}}{Dt} = \tau_{ij} \frac{\partial U_j}{\partial x_i} - \frac{\rho k^{3/2}}{l_{DES}} + \frac{\partial}{\partial x_j} \left[\left(\mu + \sigma^* \mu_t \right) \frac{\partial k}{\partial x_j} \right]$$

→→DES/OES approach

> Improvement of I_{RANS} adopted from equilibrium turbulence within DES using I_{OES} in inertial regions

$$l_{OES} = \frac{k^{1/2}}{C_{\mu}\omega}$$

DDES – avoid Modeled Stress Depletion

Hybrid Turbulence Modelling

Delayed Detached Eddy Simulation: •URANS (near body surface)

•LES (shear layer, detached flow...)

DDES-k-@-SST

DDES-k-@-OES

URANS model:

k: turbulent kinetic energy
1/:: turbulence time scale
SST: Shear-Stress-Transport limiter
of eddy viscosity
OES: Organised Eddy Simulation

$$l_{DDES} = l_{RANS} - f_d \max(0, l_{RANS} - C_{DES} \times \Delta)$$

A = max($\Delta x, \Delta y, \Delta z$)

$$f_d = \begin{cases} 0, \text{ close to wall} \\ 1, \text{ far from wall} \end{cases}$$

$$r_d = \frac{\nu + \nu_t}{S_{ij}\kappa^2 d^2} \quad f_d = 1 - tanh[(8r_d^3)]$$

$$\frac{Dk}{Dt} = P_k - C_\mu k\omega + \text{div } [(\nu + \sigma_k \nu_t) \text{ grad } k]$$

$$\frac{D\omega}{Dt} = \gamma \frac{P_k \omega}{k} - \beta \omega^2 + \text{div } [(\nu + \sigma_\omega \nu_t) \text{ grad } \omega]$$

$$+2 (1 - F_1) \sigma_{\omega 2} \frac{1}{\omega} \text{ grad } k \cdot \text{ grad } \omega$$

 $\omega = \frac{\varepsilon}{\beta^* k} \qquad \nu_t = \frac{k}{\omega}$ <u>References:</u>
Wilcox: AIAA-Journal, 31(8), 1414-1421, 1993

Menter: AIAA-Journal, 32(8), 1598-1605, 1994

Braza, Hoarau, JFS, 2006, Bourguet, Braza, 2008



3D pitching wing flow a wing – Re=10⁶



PhD G. Martinat – IMFTéquipe IFS

$$\alpha = 8^{\circ}$$
 descendant



Helicopter EC145

Iso- λ_2 surfaces coloured by ω_z vorticity







II. ST06 – OAT15A Experimental set-up and flow parameters



Flow conditions:- Mach: 0.73- Re: 3×10^6 - $\alpha = 3.5^\circ$ Transition fixed by carborundum strips at x/c = 0.07





Reduced Order Modelling

- Galerkin Projection of the Hi-Fidelity system
- Use of Hadamard's formulation for surface deformation
 on a basis of most energetic modes
- Example: The Proper Orthogonal Decomposition POD modes
- Achievements:

Description of the most important complex transfers irregular – and of aperiodic effects

by a reduced number of degrees of freedom

Possible use of ROM for shape modification in optimum design

Proper Orthogonal Decomposition:

the Karhunen-Loève (KL) expansion. Given a random vector process $\vec{u} = u_i$, KL provides the best approximation based on an energetic criterion. More precisely, considering all possible processes $\vec{\psi} = \psi_i$, the KL solution maximizes the following quantity:

$$\max_{\psi} \quad \frac{|(u,\psi)|^2}{(\psi,\psi)} = \frac{|(u,\phi)|^2}{(\phi,\phi)} \qquad (f,g) = \int_{\Omega} f(x)g^*(x)dx$$

where $\langle ., . \rangle$ represents a stochastic dot product. According to the KL theory, the solution is provided by the eigenmodes $\vec{\phi}^{(n)} = \phi_i^{(n)}$ of the second-order space-time correlations tensor and the random process can be expanded as a linear combination of these deterministic eigenvectors:

$$\int_{\Omega} \overline{u_i(x)u_j^*(x')} \phi_j(x') dx' = \lambda \phi_i(x) \qquad \qquad u_i(\vec{x},t) = \sum_{n=1}^{\infty} a^{(n)} \phi_i^{(n)}(\vec{x},t)$$

-Reconstruction

$$u_i(x,t) = \sum_k a_k \phi_i^{(k)}(x,t) \quad a_k = \int \int_{\Omega} u_i(x,t) \phi_i^*(x,t) dx dt \quad a_k a_{k'} = \delta_{kk'} \lambda_k$$

-correlations tensor

Berkooz, Holmes & Lumley, Ann. Review Fluid Mech., 1993

$$R(x,x') = \overline{u_{i}(x)u_{j}(x')} = \sum_{k} \lambda^{(k)} \phi_{i}^{(k)}(x) \phi_{j}^{(k)}(x')$$

Low Order Modelling

Galerkin projection – Navier-Stokes eqns

Incompressible flow

$$\begin{split} \int_{\Omega} \phi_m(x) \cdot \left(\frac{\partial V}{\partial t} + (V \cdot \nabla) V + \nabla p - \frac{1}{Re} \nabla^2 V \right) \mathrm{d}x &= 0, \\ \int_{\Omega} \phi_m(x) \cdot (\nabla \cdot V) \,\mathrm{d}x &= 0. \end{split}$$

Résultat : Système ODE

$$\frac{da_i(t)}{dt} = \mathcal{A}_i + \sum_{j=1}^{N_{\text{gal}}} \mathcal{B}_{ij} a_j(t) + \sum_{j=1}^{N_{\text{gal}}} \sum_{k=1}^{N_{\text{gal}}} \mathcal{C}_{ijk} a_j(t) a_k(t) + \mathcal{D}_i \frac{d\gamma}{dt} + \left(\mathcal{E}_i + \sum_{j=1}^{N_{\text{gal}}} \mathcal{F}_{ij} a_j(t) \right) \gamma + \mathcal{G}_i \gamma^2, \quad i = 1, \dots, N_{\text{gal}}.$$

Ma & Karniadakis, JFM 458, 2002

Bergmann et al, Phys. Fluids, 17, 2005,

Noack & Monkewich, JFM 523, 2005

COMPRESSIBLE FLOWS ROM: USE OF THE TRANSFORMATION $(1/\rho)$ to ensure quadratic form of the projected eqns:

Vigo, Dervieux, (2007), Bourget, Braza (Phys Fluids <u>Physics of Fluids</u>, **19**, 111701, 2007, Phys. Fluids <u>Phys.</u> <u>Fluids</u> **21**(9), pp. 111701-111701, 2009)

2. POD-Galerkin model

The compressible Navier-Stokes equations are expressed as quadratic fluxes by means of the previously defined state formulation (2), as reported in Ref. 13 for i=1,2,3,

$$\frac{\partial(1/\rho)}{\partial t} + u_{\alpha} \frac{\partial(1/\rho)}{\partial x_{\alpha}} - \frac{\partial u_{\alpha}}{\partial x_{\alpha}}(1/\rho) = 0,$$

$$\frac{\partial u_i}{\partial t} + u_\alpha \frac{\partial u_i}{\partial x_\alpha} + (1/\rho) \frac{\partial p}{\partial x_i} = (1/\rho) \frac{\partial \tau_{i\alpha}}{\partial x_\alpha},\tag{6}$$

$$\frac{\partial p}{\partial t} + \gamma p \frac{\partial u_{\alpha}}{\partial x_{\alpha}} + u_{\alpha} \frac{\partial p}{\partial x_{\alpha}} = \frac{\gamma \mu}{\Pr} \frac{\partial^2 (p/\rho)}{\partial x_{\alpha}^2} + (\gamma - 1) \frac{\partial u_{\alpha}}{\partial x_{\beta}} \tau_{\alpha\beta},$$

where $\tau_{ij} = \mu (\partial u_i / \partial x_j + \partial u_j / \partial x_i - 2/3 \partial u_\alpha / \partial x_\alpha \delta_{ij})$. Greek suband superscripts are used to specify implicit summations in previous expressions and in the following. μ is the fluid dynamic viscosity, Pr=0.72 is the Prandtl number, and δ_{ij} is the Kronecker symbol.

Interaction Fluide-Structure parois déformables



Reduced Order Modelling ROM



Galerkin projection of the transport eqns

on a basis of orthogonal most energetic modes via "Proper Orthogonal Decomposition"

Efficient formulation for Compressible

Ficticious Domain conditions approach



FIG. 7: Reference domain and modified boundary.



A. Hadamard formulation for domain deformation

In his pioneering work [57], Hadamard studied the variation of the solution of a partial differential equation with respect to its domain Ω_{γ} in the neighborhood of a reference domain Ω_0 . He demonstrated that this variation can be well defined on the reference domain. This Hadamard derivative is the solution of a differentiated partial differential equation with a boundary source term distributed on $\Gamma_0 = \partial \Omega_0$ which is linear with respect to the boundary variation. Following Hadamard, the boundary variation is parameterized by a normal displacement γn (figure 7):

$$\Gamma_{\gamma} = \{ \boldsymbol{x} = \boldsymbol{x}_0 + \gamma(\boldsymbol{x}_0)\boldsymbol{n}(\boldsymbol{x}_0), \forall \boldsymbol{x}_0 \in \Gamma_0 \}.$$
(26)

In the following, ${\boldsymbol R}$ denotes the differential volumic residual:

$$\boldsymbol{R}\left(\boldsymbol{v}\right) = \boldsymbol{v}_{,t} + \boldsymbol{F}_{\alpha,\alpha} - \boldsymbol{F}_{\alpha,\alpha}^{\mathrm{vis}},\tag{27}$$



For a given geometry Ω_{γ} defined by γ , $v^{\text{NS}}(\gamma)$ is the set of flow variables solving the HF Navier-Stokes equations as introduced in (2). In an integral formulation where Ψ_1 , Ψ_2 and * correspond respectively to two test functions and to a dimensionally consistent scalar product in \mathbb{R}^4 , this can be written as follows:

$$\boldsymbol{v}^{\mathrm{NS}} = \begin{bmatrix} \rho^{\mathrm{NS}} \\ \rho^{\mathrm{NS}} \boldsymbol{u}_1^{\mathrm{NS}} \\ \rho^{\mathrm{NS}} \boldsymbol{u}_2^{\mathrm{NS}} \\ \rho^{\mathrm{NS}} \boldsymbol{e}_{\mathrm{NS}} \end{bmatrix}, \qquad (29)$$

$$\boldsymbol{v} = \boldsymbol{v}^{\mathrm{NS}}(\gamma) \iff \int_{\Omega_{\gamma}} \boldsymbol{\Psi}_{1} \ast \boldsymbol{R}(\boldsymbol{v}) \, d\boldsymbol{x} + \int_{\Gamma_{\gamma}} \boldsymbol{\Psi}_{2} \ast \boldsymbol{C}(\boldsymbol{v}) \, d\boldsymbol{\sigma} = 0, \ \forall \boldsymbol{\Psi}_{1}, \boldsymbol{\Psi}_{2}.$$
(30)

The Hadamard's formulation

For a variation $\delta \gamma$ of the shape, the variation δv^{NS} of the flow unknown v^{NS} is approximated by the following truncated Taylor formula that is second-order accurate with respect to an adhoc norm of $\delta \gamma$:

$$\delta \boldsymbol{v}^{\mathrm{NS}}\left(\boldsymbol{\gamma}, \delta\boldsymbol{\gamma}\right) = \boldsymbol{v}^{\mathrm{NS}}\left(\boldsymbol{\gamma} + \delta\boldsymbol{\gamma}\right) - \boldsymbol{v}^{\mathrm{NS}}\left(\boldsymbol{\gamma}\right) \approx \frac{\partial \boldsymbol{v}^{\mathrm{NS}}}{\partial\boldsymbol{\gamma}}\left(\boldsymbol{\gamma}\right)\delta\boldsymbol{\gamma}.$$
(31)

RHS in (31) is obtained from the total derivative of the flow equation (30):

$$\int_{\Omega_{\gamma}} \Psi_{1} * \frac{\partial \boldsymbol{R}}{\partial \boldsymbol{v}} \frac{\partial \boldsymbol{v}}{\partial \gamma} \delta \gamma d\boldsymbol{x} + \int_{\Gamma_{\gamma}} \Psi_{2} * \frac{\partial \boldsymbol{C}}{\partial \boldsymbol{v}} \frac{\partial \boldsymbol{v}}{\partial \gamma} \delta \gamma d\sigma + \int_{\Gamma_{\gamma}} \Psi_{1} * \boldsymbol{R}(\boldsymbol{v}) \,\delta \gamma d\sigma + \int_{\Gamma_{\gamma}} \Psi_{2} * \mathcal{N}\boldsymbol{C}(\boldsymbol{v}) \,\delta \gamma d\sigma = 0, \,\forall \Psi_{1}, \Psi_{2}, \quad (32)$$

where \mathcal{H} is Γ_{γ} curvature. Since $v^{\text{NS}}(\gamma)$ is solution of the flow system for γ , then the third and fifth integrals in (32) vanish.

In the following, a small perturbation $\delta \gamma$ is considered about $\gamma = 0$:

$$\boldsymbol{v}^{\mathrm{NS}}\left(\delta\gamma\right) = \boldsymbol{v}^{\mathrm{NS}}\left(0\right) + \delta\boldsymbol{v}^{\mathrm{NS}}\left(0,\delta\gamma\right) \tag{33}$$

and
$$\delta \boldsymbol{v}^{\text{NS}}(0,\delta\gamma) \approx \frac{\partial \boldsymbol{v}^{\text{NS}}}{\partial\gamma}(0)\,\delta\gamma.$$
 (34)

Capturing of irregular effects in the near-wall vorticity patterns by Reduced Order Modelling



POD analysis of the near-wake structure Re=140,000 From OES – IMFT's Circular Cylinder DESIDER EU program



FIG. 6.21 - Pourcentage d'énergie des 100 premiers modes

El Akoury, Braza et al, 2009,

in Notes on Num. Fluid Mech. and multidiscipl. design, eds, Haase et al, Springer



mode 1, correspondance ar champ moyen mode 2 mode 2 mode 3 mode 3 mode 4













First application: DES/OES

IMFT's Circular cylinder

Capturing not only the von Karman Vortices but also the shear-layer Instability: Kelvin-Helmholtz vortices Past the separation point By POD reconstruction

El Akoury et al, *Notes on Num. Fluid Mech. And Multidisciplinary Design Vol.* **103**



POD reconstruction of the Kelvin-Helmholtz vortices

Nanorotors coaxiaux: caractérisation et optimisation





- Montage expérimental sur nano-balance de précision
- Calcul Navier-Stokes par méthode MRF





Figure 1: Schematic representation of the flow configuration (a). The frame origin is on the trailing edge at the half of the plate's span. View of phase-averaged iso-vorticity field, CFD simulations by Ouvrard et al (2010), (b).



CONFIGURATION GENERIQUE DE VOLET DEFORMABLE

Figure 2: View of the experimental set-up and of an instantaneous 3D velocity field

Tomo-PIV



3.1 Reynolds averaged quantities



Figure 3: Reynolds averaged quantities measured by Tomo-PIV: streamwise U velocity and vertical V velocity.

S4 wind tunnel IMFT

Post-doc EMMAV E. Deri





MORPHING DE VOLET DEFORMABLE PAR ALLIAGES A MEMOIRE DE FORME – « SHAPE MEMORY ALLOYS » – INSTRUMENTE AU LAPLACE

AMELIORATION DE LA VITESSE DE REFROIDISSEMENT -

ACTIONNEMENT PLUS RAPIDE

MESURE DU CHAMPS DE VITESSE INSTATIONNAIRE DANS LA REGION PROCHE EN SOUFFLERIE S4 - IMFT

2 Films



MERCI DE VOTRE ATTENTION